

ElementSets from MeshConnectivity

NeighborVerticesInFace, Faces, VertexOneRing from Neighborhoods(M)

$M : \text{FaceMesh}$

$x_i \in \mathbb{R}^3$

$V, E, F = \text{ElementSets}(M)$

$\text{VertexNormal}(i) = \frac{w}{\|w\|}$

where

$i \in V$

$w = \sum_{f \in \text{Faces}(i)} (x_j - x_i) \times (x_k - x_i) \quad \text{where } j, k = \text{NeighborVerticesInFace}(f, i)$

$\text{CalcNorm}(i, v, n, \sigma_c, \sigma_s) = w_c \cdot w_s$

where

$i, v \in \mathbb{Z}, \text{vertices}$

$\sigma_c, \sigma_s \in \mathbb{R}$

$n \in \mathbb{R}^3$

$t = \|x_i - x_v\|$

$h = \langle n, x_v - x_i \rangle$

$w_c = e^{-\frac{t^2}{2\sigma_c^2}}$

$w_s = e^{-\frac{h^2}{2\sigma_s^2}}$

$\text{CalcS}(i, v, n, \sigma_c, \sigma_s) = \text{CalcNorm}(i, v, n, \sigma_c, \sigma_s) \cdot h$

where

$i, v \in \mathbb{Z}, \text{vertices}$

$\sigma_c, \sigma_s \in \mathbb{R}$

$n \in \mathbb{R}^3$

$h = \langle n, x_v - x_i \rangle$

$\text{DenoisePoint}(i) = x_i + n \cdot \left( \frac{s}{\text{norm}} \right)$

where

$i \in V$

$n = \text{VertexNormal}(i)$

$\sigma_c = \text{CalcSigmaC}(i)$

$\text{neighbors} = \text{AdaptiveVertexNeighbor}(i, \{i\}, \sigma_c)$

$\sigma_s = \text{CalcSigmaS}(i, \text{neighbors})$

$s = \sum_{v \in \text{neighbors}} \text{CalcS}(i, v, n, \sigma_c, \sigma_s)$

$\text{norm} = \sum_{v \in \text{neighbors}} \text{CalcNorm}(i, v, n, \sigma_c, \sigma_s)$

$\text{CalcSigmaC}(i) = \min(\{\|x_i - x_v\| \mid v \in \text{VertexOneRing}(i)\})$  where  $i \in V$

$\text{CalcSigmaS}(i, N) = \begin{cases} \sqrt{\text{offset} + 10^{-12}} & \text{if } \sqrt{\text{offset}} < 10^{-12} \\ \sqrt{\text{offset}} & \text{otherwise} \end{cases}$

where

$i \in V$

$N \subset V$

$n = \text{VertexNormal}(i)$

$\text{avg} = \sum_{v \in N} \frac{t}{|N|} \quad \text{where } t = \sqrt{((x_v - x_i) \cdot n)^2}$

$\text{sqs} = \sum_{v \in N} (t - \text{avg})^2 \quad \text{where } t = \sqrt{((x_v - x_i) \cdot n)^2}$

$\text{offset} = \frac{\text{sqs}}{|N|}$

$\text{AdaptiveVertexNeighbor}(i, n, \sigma) = \begin{cases} n & \text{if } |n| = |\text{target}| \\ \text{AdaptiveVertexNeighbor}(i, \text{target}, \sigma) & \text{otherwise} \end{cases}$

where

$i \in V$

$\sigma \in \mathbb{R}$

$n \subset V$

$\text{target} = \{v \mid v \in \text{VertexOneRing}(n), \|x_i - x_v\| < 2\sigma\} \cup n$